

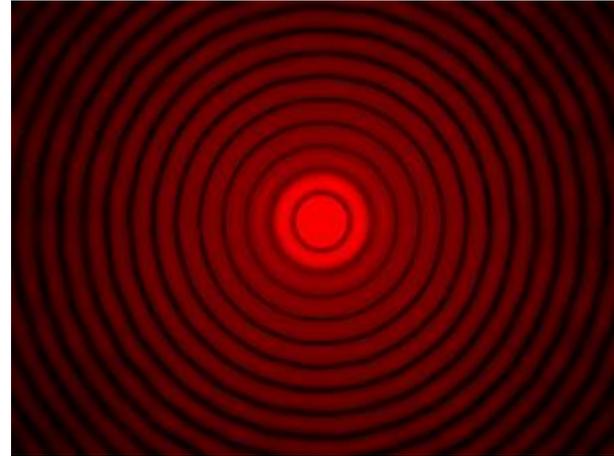
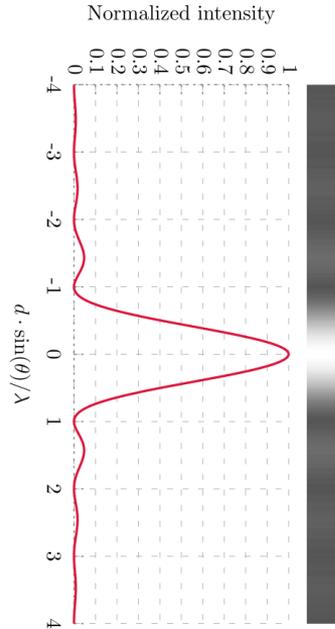
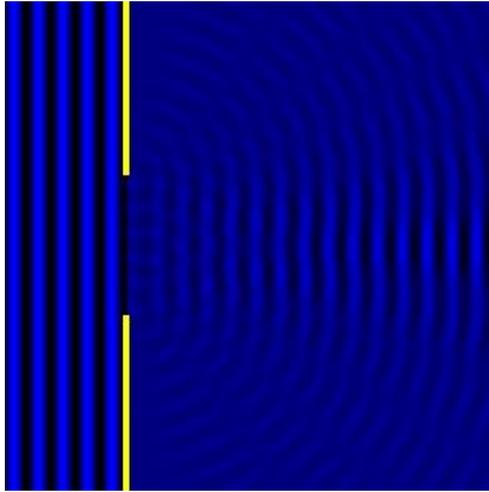
Superresolution fluorescence microscopy

Leonid Keselman, Daniel Fernandes

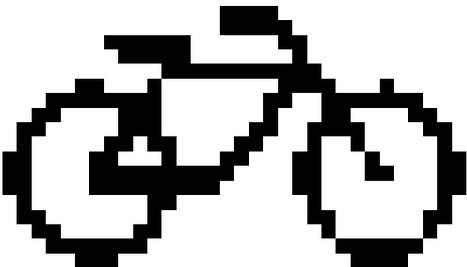
Overview

1. What is “super-resolution”
 - a. Diffraction
 - b. STORM
2. Compressed Sensing
 - a. Applied to STORM
3. Light Sheet Imaging
 - a. Lattice-Light Sheets

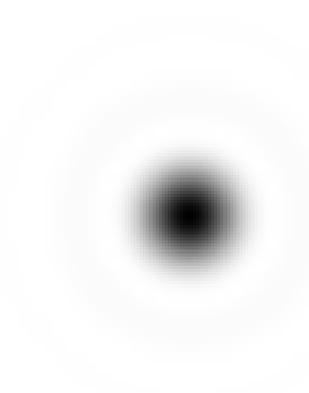
Natural Resolution Limits: Diffraction



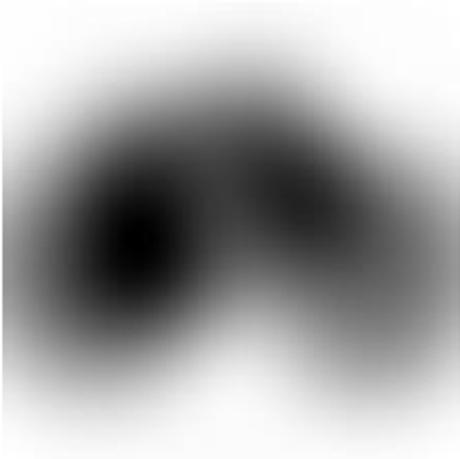
Natural Resolution Limits: Diffraction



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sources: font-awesome fa-bicycle

Natural Resolution Limits: Diffraction

For typical cameras

$$d = 1.22 * \lambda * f\#$$

Raleigh Criterion

iPhone 7:
= $1.22 * 650\text{nm} * f/1.8$
= $1.4 \mu\text{m}$
pixels are only $1.22 \mu\text{m}$!

For microscopes

$$d = \frac{\lambda}{2n \sin \theta} = \frac{\lambda}{2 NA}$$

Abbe diffraction limit

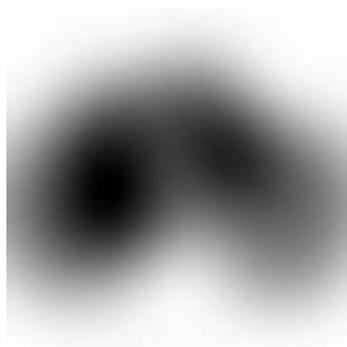
Typical Limit:
= $500\text{nm}/(2 * 1.25)$
= $0.2 \mu\text{m} = 200\text{nm}$
Microtubules are $\sim 24\text{nm}$

NA is typically 0.1-0.4 for common lenses in air, up to 1.0-1.5 for oil lenses.

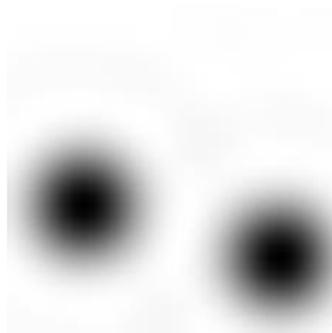
STORM: Stochastic Optical Reconstruction Microscopy

Rust, Bates, Zhuang. "Stochastic optical reconstruction microscopy (STORM) provides sub-diffraction-limit image resolution." *Nature Methods* 3.10 (2006)

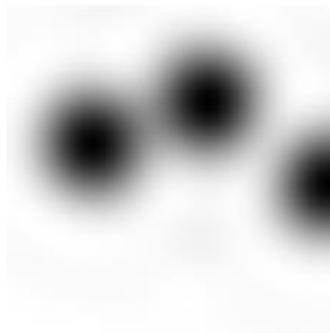
All pixels "on":



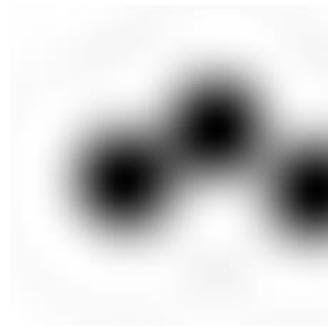
Random 1% of
pixels "on"



Random 1% of
pixels "on"



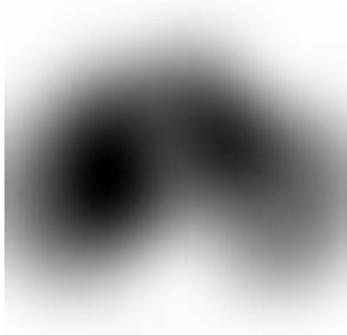
Random 1% of
pixels "on"



STORM: Stochastic Optical Reconstruction Microscopy

Rust, Bates, Zhuang. "Stochastic optical reconstruction microscopy (STORM) provides sub-diffraction-limit image resolution." *Nature Methods* 3.10 (2006)

All pixels "on":



1 reading



100 readings

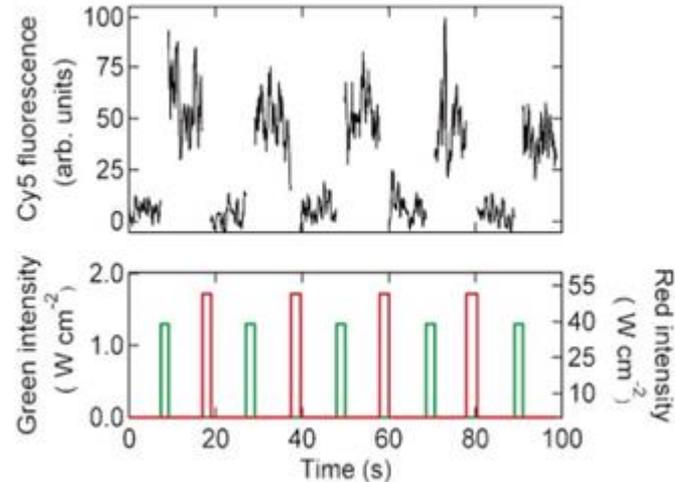
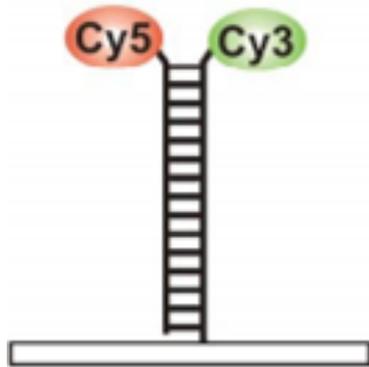


1000 readings



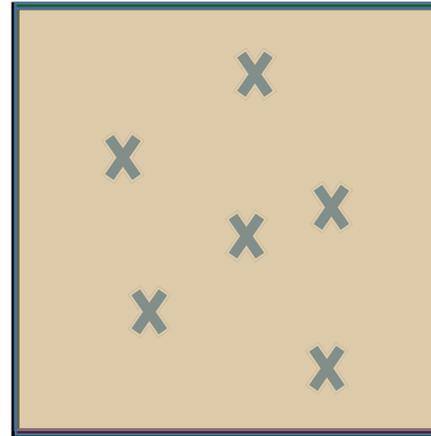
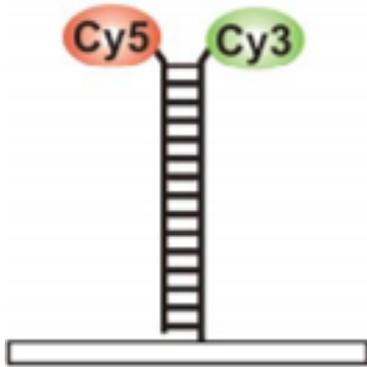
STORM: Stochastic Optical Reconstruction Microscopy

Bates, Blosser, Zhuang. "Short-range spectroscopic ruler based on a single-molecule optical switch." *Physical review letters* 94.10 (2005)



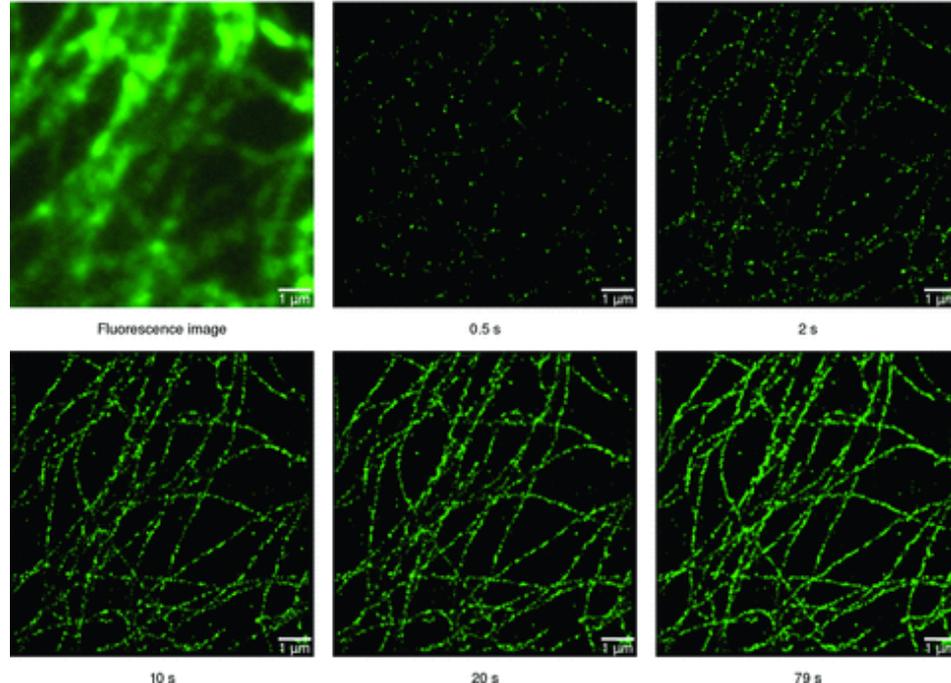
STORM: Stochastic Optical Reconstruction Microscopy

Bates, Blosser, Zhuang. "Short-range spectroscopic ruler based on a single-molecule optical switch." *Physical review letters* 94.10 (2005)



STORM: Stochastic Optical Reconstruction Microscopy

Wolter, Steve, et al. "Real-time computation of subdiffraction-resolution fluorescence images." *Journal of microscopy* 237.1 (2010)



Compressed Sensing (a.k.a. Sparse Sampling)

If your data is “compressible”, you can take just a handful of random measurements, and, using “simple” math, you can reconstruct your data (with minimal error and high probability)

Emmanuel Candes and Terence Tao. "Near-optimal signal recovery from random projections: Universal encoding strategies?." *arXiv:math/0410542* (2004)

$$\min \|x\|_{\ell_1} \quad \text{subject to} \quad \|Ax - y\|_{\ell_2} \leq \epsilon.$$

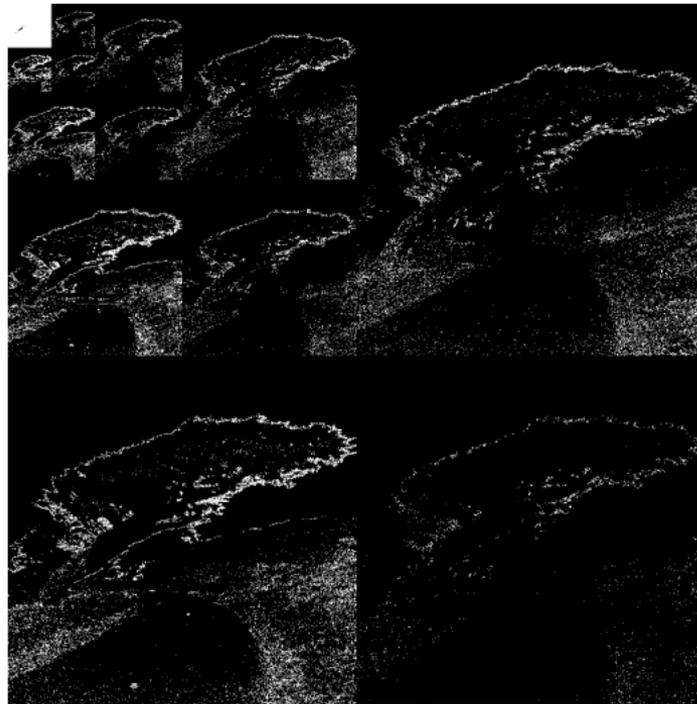
Compressed Sensing (a.k.a. Sparse Sampling)

	1	2	3	4	5	6
1	X	X		X		
0		X	X	X		
2	X			X		X

Compressed Sensing (a.k.a. Sparse Sampling)

	1	2	3	4	5	6
1	X	0		0		
0		0	0	0		
2	X			0		X

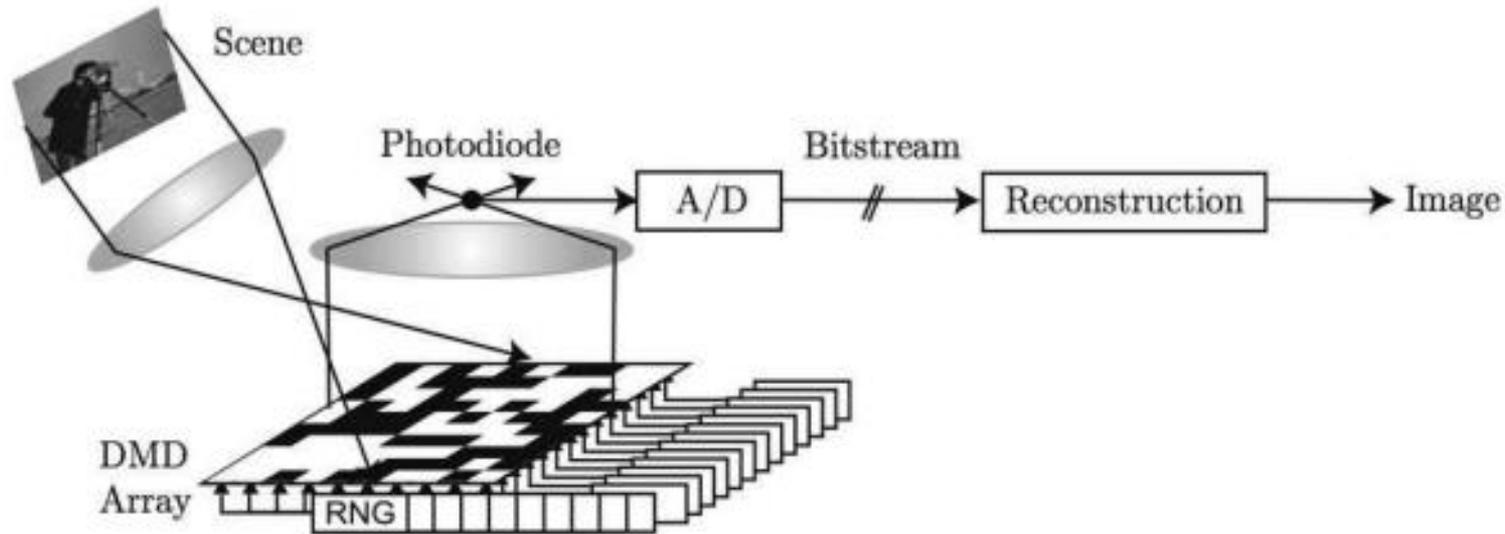
Compressed Sensing (a.k.a. Sparse Sampling)



Davenport, Duarte, Eldar, Kutyniok , *Introduction to Compressed Sensing*

Compressed Sensing

Duarte, et al. *Single-Pixel Imaging via Compressive Sampling*. (2008)

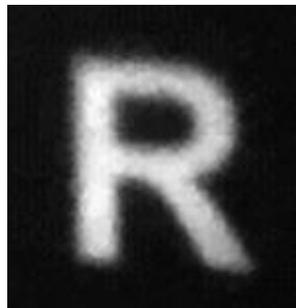


Compressed Sensing

Real Picture
(65,536 pixels)



CS Reconstruction
(3,300 samples)



CS Reconstruction
(1,300 samples)



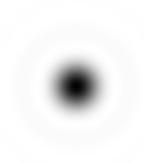
CS Reconstruction
(6,500 samples)



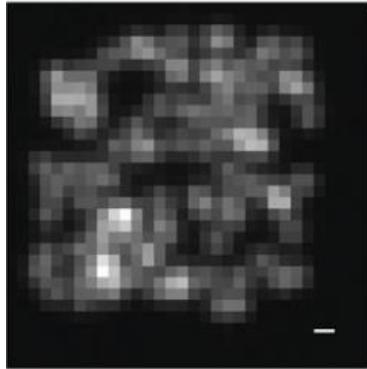
Faster STORM using compressed sensing

Zhu, et al. "Faster STORM using compressed sensing." *Nature Methods* (2012)

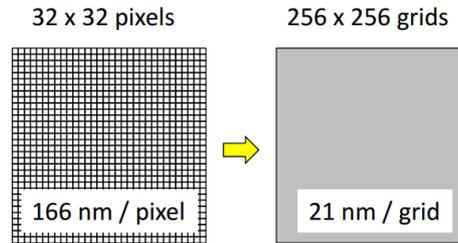
1. Acquire PSF



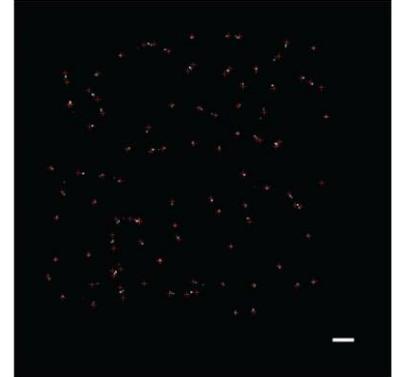
2. Get Image



3. Increase Grid



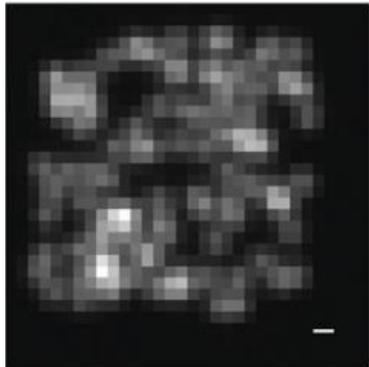
4. Solve CS problem



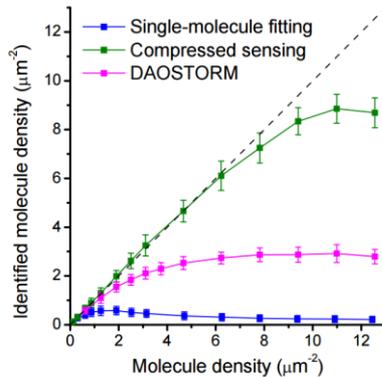
Faster STORM using compressed sensing

Zhu, et al. "Faster STORM using compressed sensing." *Nature Methods* (2012)

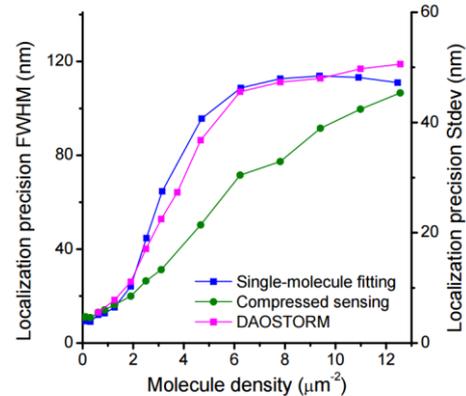
Denser Images!



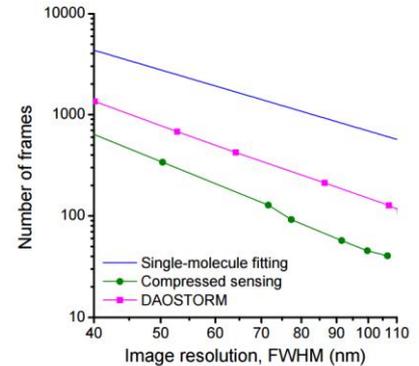
Many times denser



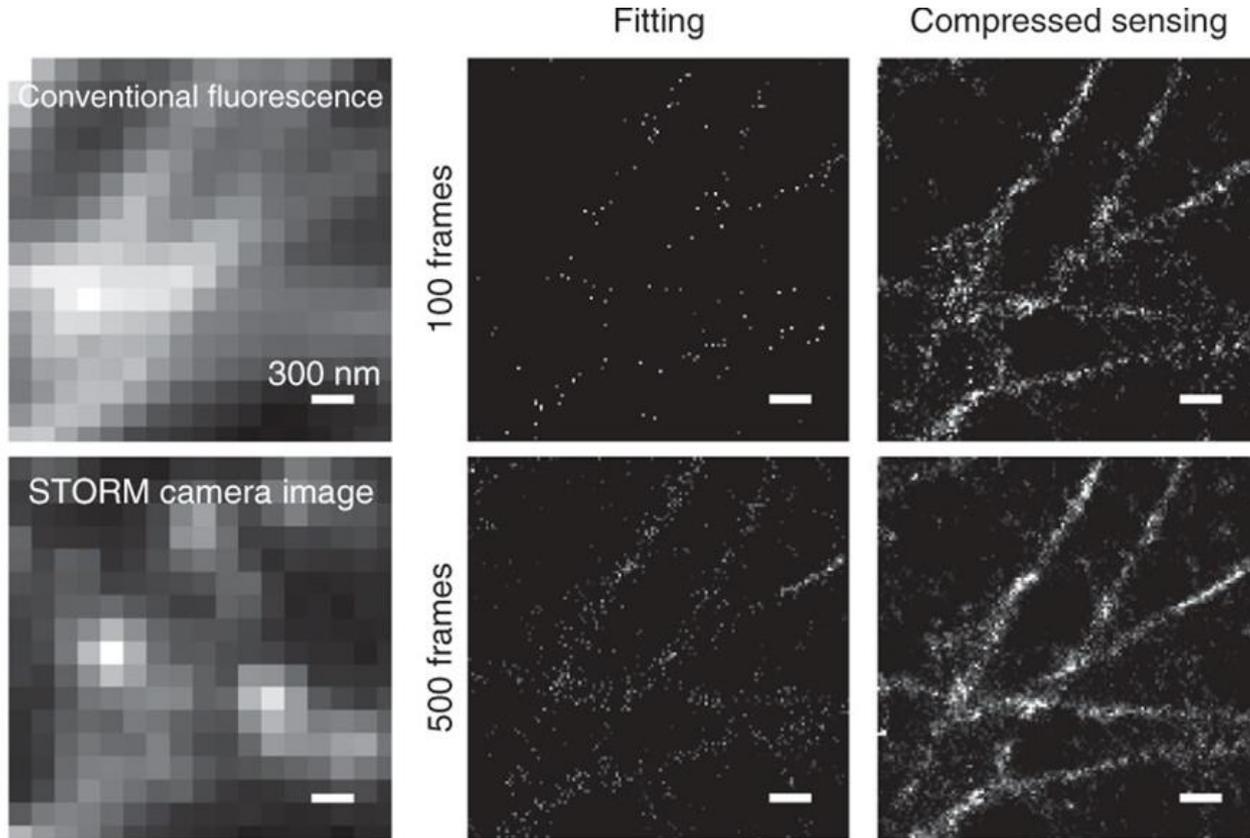
More precise

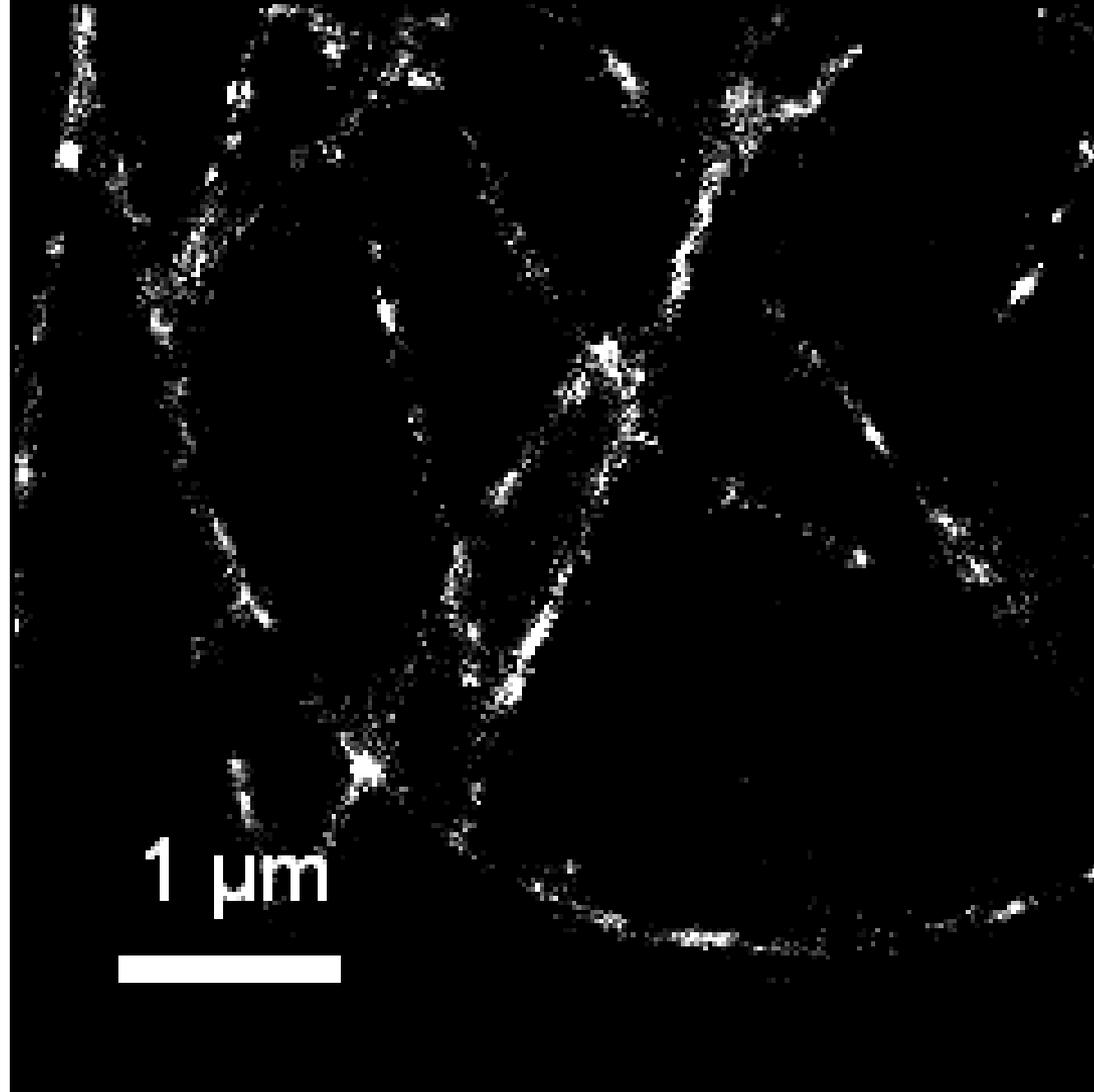


Faster imaging



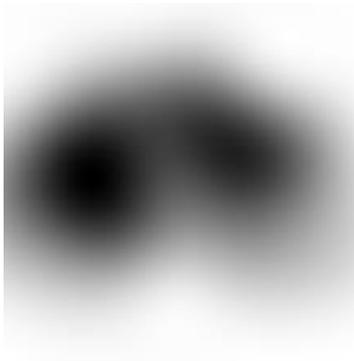
Faster STORM using compressed sensing





Faster STORM using compressed sensing

40% pixels on



40% on, CS Solve



CS
50 readings
4% Density



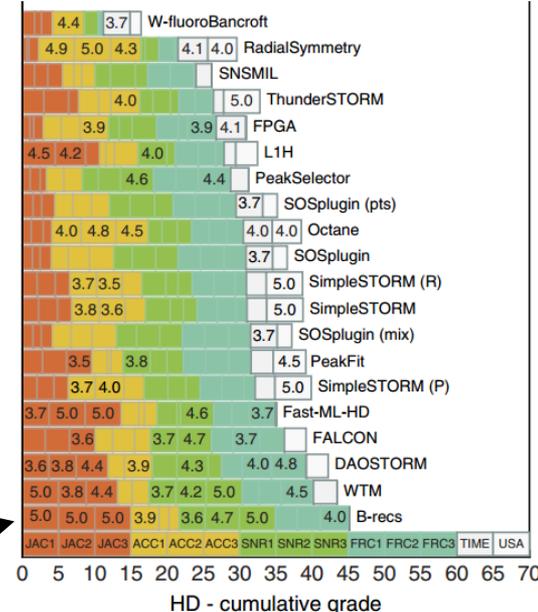
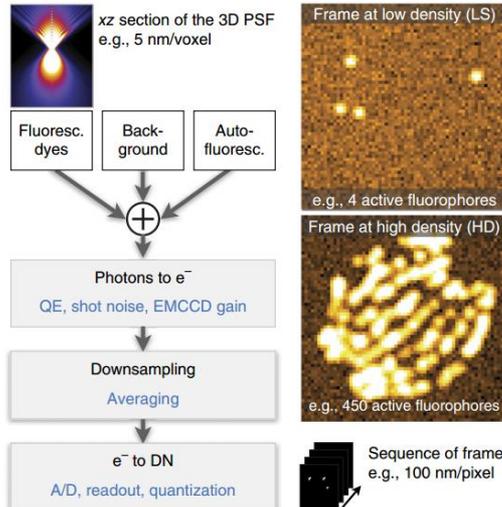
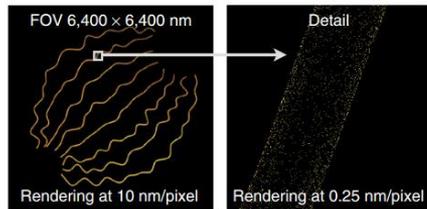
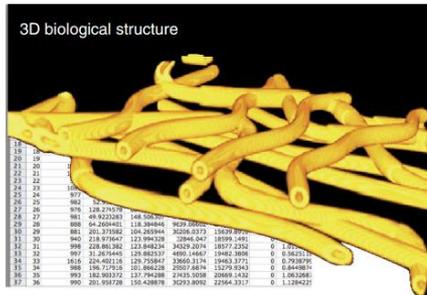
Classic
1000 readings
~0.8% Density



<https://github.com/leonidk/cs371>

Quantitative Comparison

Sage, Daniel, et al. "Quantitative evaluation of software packages for single-molecule localization microscopy." *Nature Methods* 12.8 (2015)



<https://github.com/hrouault/Brecs>

Extra Slides

Faster STORM using compressed sensing

Solve

$$w_0(\text{img}_0) + \dots + w_{205}(\text{img}_{205}) + \dots + w_{819}(\text{img}_{819}) + \dots = \text{img}_{\text{target}}$$

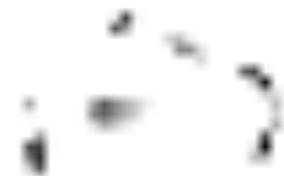
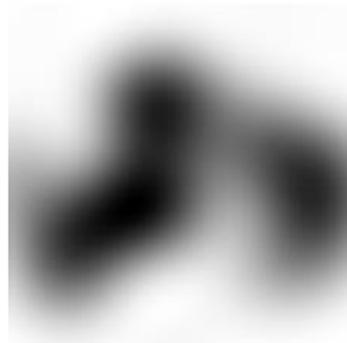
With

$$\min \|\mathbf{w}\|_1$$

Gives

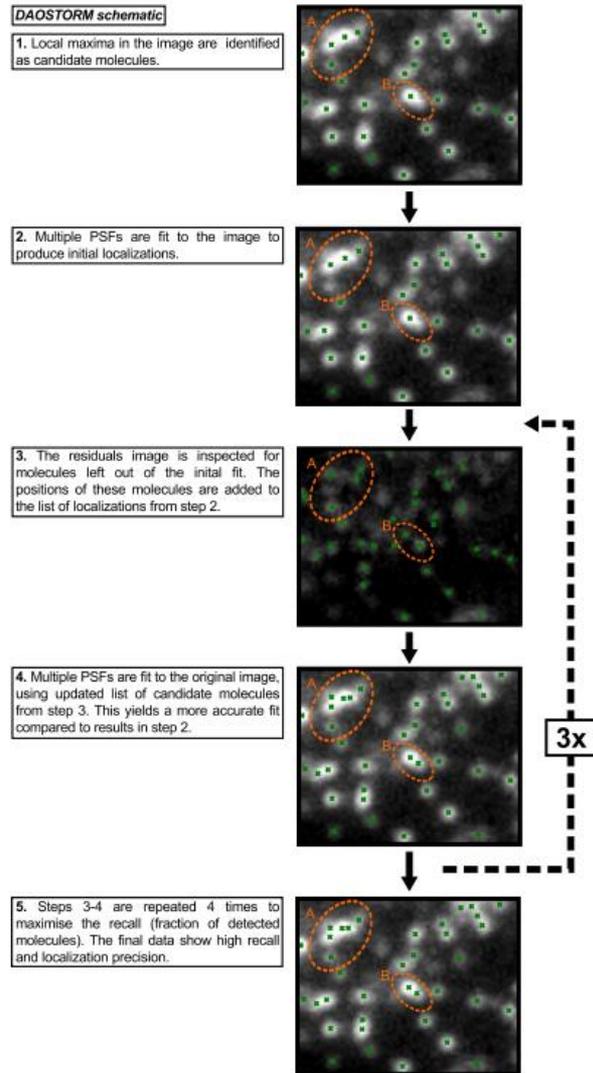
$$\mathbf{w} \in \mathbb{R}^{1024} \Rightarrow \mathbf{w} \in \mathbb{R}^{32 \times 32}$$

$\mathbf{w} =$



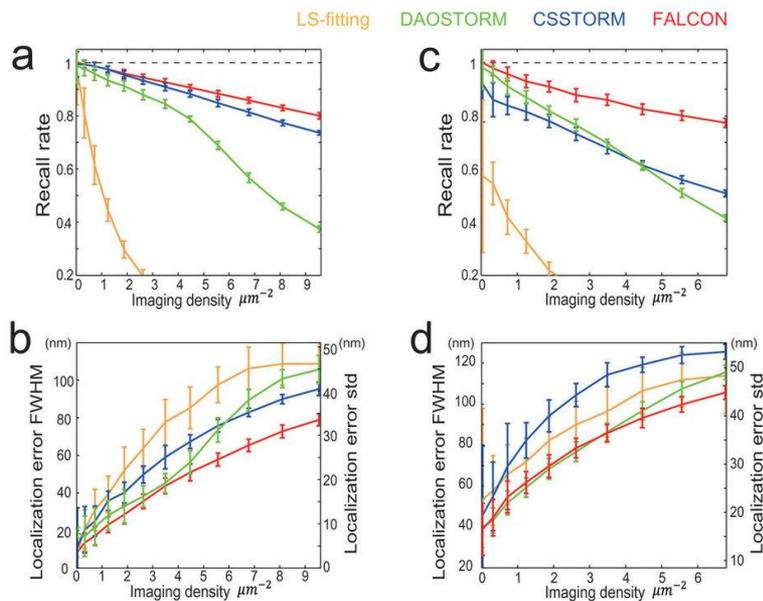
DAOSTORM

Stetson, Peter B. "DAOPHOT: A computer program for crowded-field stellar photometry." *Publications of the Astronomical Society of the Pacific* 99.613 (1987).



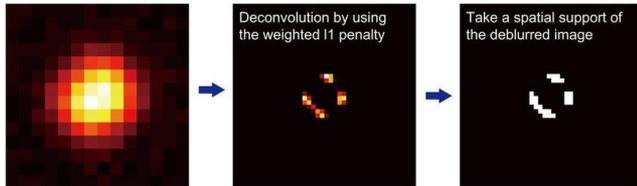
FALCON

Min, Junhong, et al. "FALCON: fast and unbiased reconstruction of high-density super-resolution microscopy data." *Scientific reports* 4 (2014)

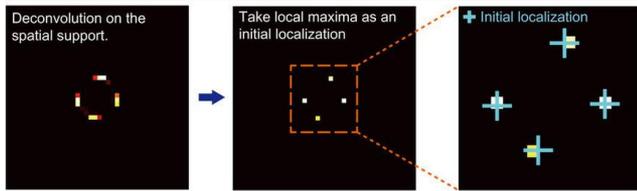


Algorithm schematic diagram

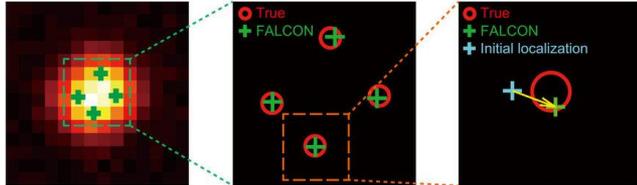
1. Deconvolution with sparsity priors
 A deblurred image is generated by using sparsity-promoting priors (weighted l1 norm) on a sub-pixel grid.



2. Deconvolution with fixed spatial support
 Deconvolution by minimizing the least-squares criterion on a fixed spatial support



3. Continuous refinement
 Initial localizations are refined by alternatively updating positions and brightnesses. Yellow arrows show directions of refinement.



Supplementary Figure: Switching kinetics

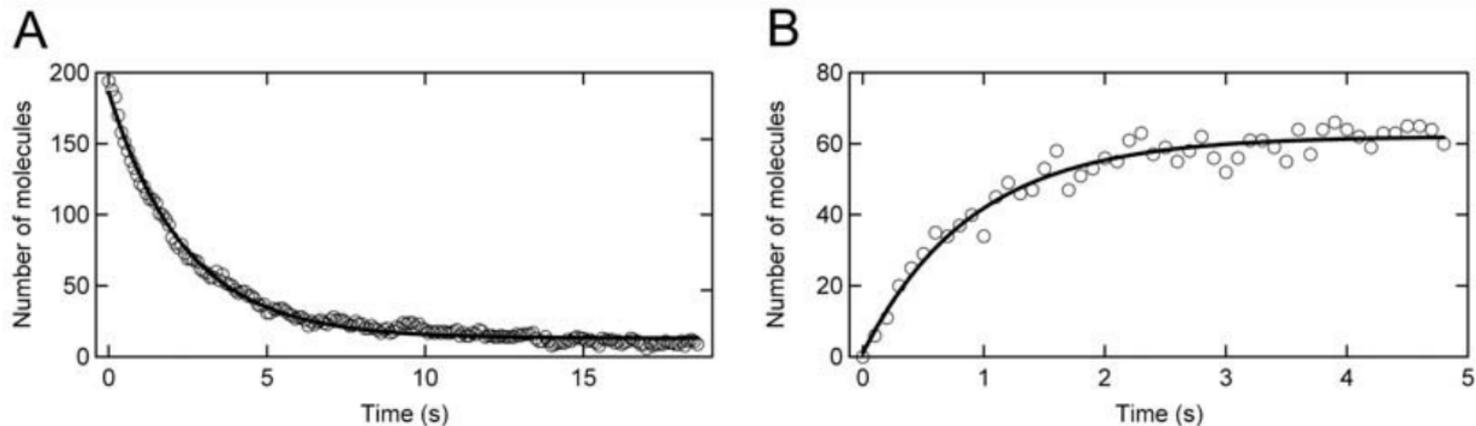


Figure S1. The first-order switching kinetics of the molecular switch. **A**, The number of molecules remaining fluorescent as a function of time after the green laser was turned off. A single exponential fit of the data (solid line) gives $k_{\text{off}} = 0.4 \text{ s}^{-1}$. **B**, The number of molecules that were converted back to the fluorescent state as a function of time after the green laser was turned on. A single exponential fit (solid line) gives the observed rate constant for switching Cy5 on ($k_{\text{on_obs}} = 1.1 \text{ s}^{-1}$). Considering the competing actions of the red and green lasers, the actual rate constant k_{on} for switching the dye on by the green laser is equal to $k_{\text{on_obs}} - k_{\text{off}}$. Data in **A** and **B** are not from the same experiment.

Abstract

Suppose we are given a vector f in a class $\mathcal{F} \subset \mathbb{R}^N$, e.g. a class of digital signals or digital images. How many linear measurements do we need to make about f to be able to recover f to within precision ϵ in the Euclidean (ℓ_2) metric?

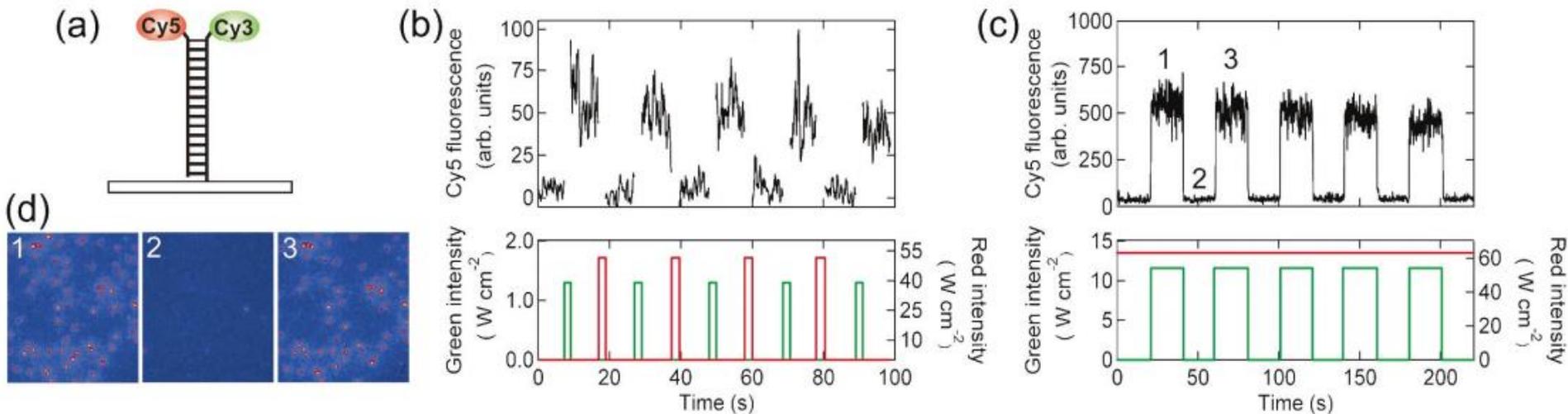
This paper shows that if the objects of interest are sparse in a fixed basis or compressible, then it is possible to reconstruct f to within very high accuracy from a small number of random measurements by solving a simple linear program. More precisely, suppose that the n th largest entry of the vector $|f|$ (or of its coefficients in a fixed basis) obeys $|f|_{(n)} \leq R \cdot n^{-1/p}$, where $R > 0$ and $p > 0$. Suppose that we take measurements $y_k = \langle f, X_k \rangle$, $k = 1, \dots, K$, where the X_k are N -dimensional Gaussian vectors with independent standard normal entries. Then for each f obeying the decay estimate above for some $0 < p < 1$ and with overwhelming probability, our reconstruction f^\sharp , defined as the solution to the constraints $y_k = \langle f^\sharp, X_k \rangle$ with minimal ℓ_1 norm, obeys

$$\|f - f^\sharp\|_{\ell_2} \leq C_p \cdot R \cdot (K/\log N)^{-r}, \quad r = 1/p - 1/2.$$

There is a sense in which this result is optimal; it is generally impossible to obtain a higher accuracy from any set of K measurements whatsoever. The methodology extends to various other random measurement ensembles; for example, we show that similar results hold if one observes few randomly sampled Fourier coefficients of f . In fact, the results are quite general and require only two hypotheses on the measurement ensemble which are detailed.

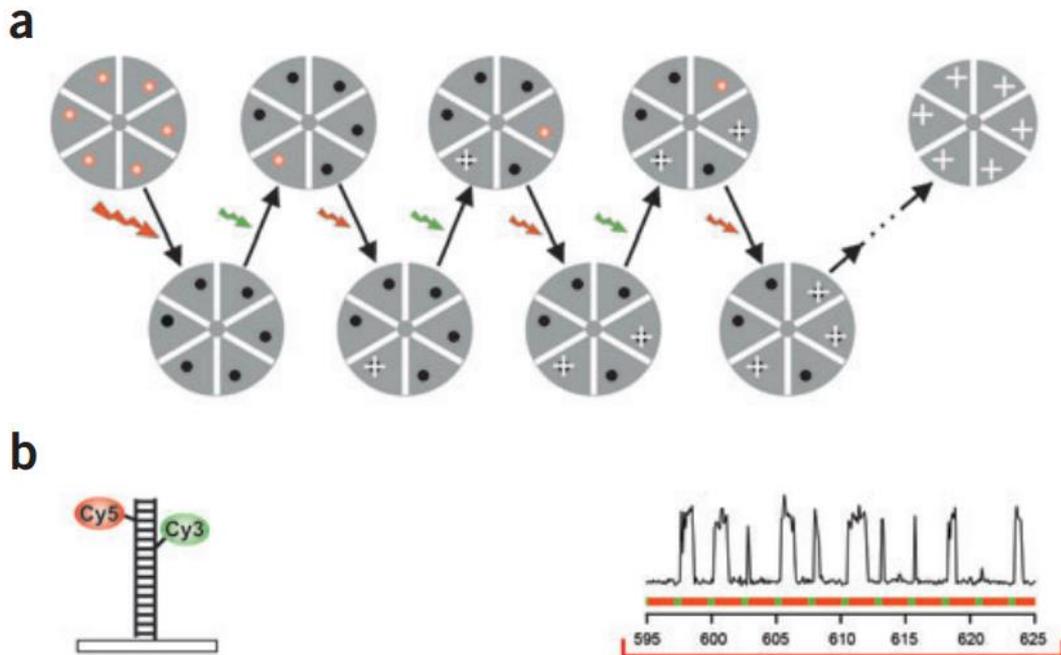
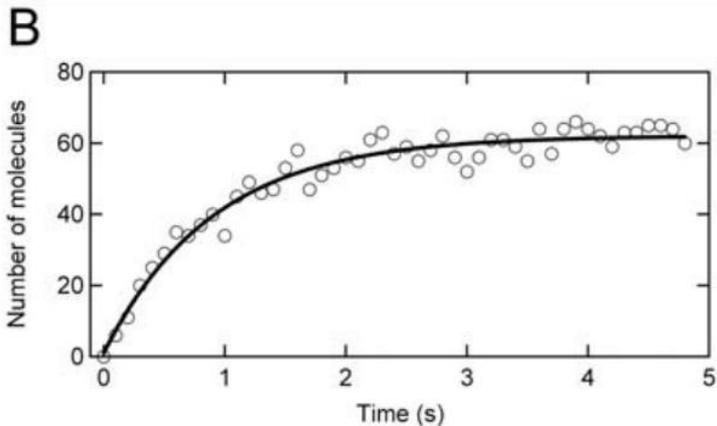
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